

Erroneous Non blocking Atomic *Commitment* Protocol (ACP-NB)

The mistake is to deliver a broadcast message locally \*before\* it has been forwarded to other participants.

This protocol does not satisfy the consistency property *AC1*

EXTENDS *ACP\_SB*

Participants type is extended with a “forward” variable.

Coordinator type is unchanged.

$$\begin{aligned} \text{TypeInvParticipantNB} &\triangleq \text{participant} \in [ \\ &\quad \text{participants} \rightarrow [ \\ &\quad \quad \text{vote} \quad : \{\text{yes}, \text{no}\}, \\ &\quad \quad \text{alive} \quad : \text{BOOLEAN}, \\ &\quad \quad \text{decision} : \{\text{undecided}, \text{commit}, \text{abort}\}, \\ &\quad \quad \text{faulty} \quad : \text{BOOLEAN}, \\ &\quad \quad \text{voteSent} : \text{BOOLEAN}, \\ &\quad \quad \text{forward} : [\text{participants} \rightarrow \{\text{notsent}, \text{commit}, \text{abort}\}] \\ &\quad ] \\ &] \end{aligned}$$

$$\text{TypeInvNB} \triangleq \text{TypeInvParticipantNB} \wedge \text{TypeInvCoordinator}$$

Initially, participants have not forwarded anything yet

$$\begin{aligned} \text{InitParticipantNB} &\triangleq \text{participant} \in [ \\ &\quad \text{participants} \rightarrow [ \\ &\quad \quad \text{vote} \quad : \{\text{yes}, \text{no}\}, \\ &\quad \quad \text{alive} \quad : \{\text{TRUE}\}, \\ &\quad \quad \text{decision} : \{\text{undecided}\}, \\ &\quad \quad \text{faulty} \quad : \{\text{FALSE}\}, \\ &\quad \quad \text{voteSent} : \{\text{FALSE}\}, \\ &\quad \quad \text{forward} : [\text{participants} \rightarrow \{\text{notsent}\}] \\ &\quad ] \\ &] \end{aligned}$$

$$\text{InitNB} \triangleq \text{InitParticipantNB} \wedge \text{InitCoordinator}$$

Participant statements that realize a better broadcast

*forward*(*i*, *j*): forwarding of the predecision from participant *i* to participant *j*

IF  
 participant *i* is alive  
 participant *i* has received a decision and has decided (it shouldn't have decided yet)  
 participant *i* has not yet forwarded this decision to participant *j*  
 THEN  
 participant *i* forwards the decision to participant *j*

$$\begin{aligned} \text{forward}(i, j) &\triangleq \wedge i \neq j \\ &\quad \wedge \text{participant}[i].\text{alive} \\ &\quad \wedge \text{participant}[i].\text{decision} \neq \text{notsent} \\ &\quad \wedge \text{participant}[i].\text{forward}[j] = \text{notsent} \\ &\quad \wedge \text{participant}' = [\text{participant EXCEPT ![}i] = \\ &\quad \quad [ @ EXCEPT !.\text{forward} = \\ &\quad \quad [ @ EXCEPT ![}j] = \text{participant}[i].\text{decision} \\ &\quad ] \\ &] \end{aligned}$$

$\wedge$  UNCHANGED  $\langle$  coordinator  $\rangle$

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decideOnForward(i, j): participant i receives decision from participant j
IF
  participant i is alive
  participant i has yet to receive a decision
  participant j has forwarded its decision to participant i
THEN
  participant i decides in accordance with participant j's decision (it should only predecide)

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$$\begin{aligned}
\textit{decideOnForward}(i, j) \triangleq & \wedge i \neq j \\
& \wedge \textit{participant}[i].\textit{alive} \\
& \wedge \textit{participant}[i].\textit{decision} = \textit{undecided} \\
& \wedge \textit{participant}[j].\textit{forward}[i] \neq \textit{notsent} \\
& \wedge \textit{participant}' = [\textit{participant} \text{ EXCEPT } ![i] = \\
& \quad [@\text{ EXCEPT } !.\textit{decision} = \textit{participant}[j].\textit{forward}[i]] \\
& \quad ] \\
& \wedge \text{UNCHANGED } \langle \textit{coordinator} \rangle
\end{aligned}$$

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abortOnTimeout(i): conditions for a timeout are simulated
IF
  participant is alive and undecided and coordinator is not alive
  coordinator died before sending decision to all participants who are alive
  all dead participants died before forwarding decision to a participant who is alive
THEN
  decide abort

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$$\begin{aligned}
\textit{abortOnTimeout}(i) \triangleq & \wedge \textit{participant}[i].\textit{alive} \\
& \wedge \textit{participant}[i].\textit{decision} = \textit{undecided} \\
& \wedge \neg \textit{coordinator}.\textit{alive} \\
& \wedge \forall j \in \textit{participants} : \textit{participant}[j].\textit{alive} \Rightarrow \textit{coordinator}.\textit{broadcast}[j] = \textit{notsent} \\
& \wedge \forall j, k \in \textit{participants} : \neg \textit{participant}[j].\textit{alive} \wedge \textit{participant}[k].\textit{alive} \Rightarrow \textit{participant}[j].\textit{forward}[k] = \textit{notsent} \\
& \wedge \textit{participant}' = [\textit{participant} \text{ EXCEPT } ![i] = [@\text{ EXCEPT } !.\textit{decision} = \textit{abort}]] \\
& \wedge \text{UNCHANGED } \langle \textit{coordinator} \rangle
\end{aligned}$$


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FOR *N* PARTICIPANTS

$$\begin{aligned}
\textit{parProgNB}(i, j) \triangleq & \vee \textit{parProg}(i) \\
& \vee \textit{forward}(i, j) \\
& \vee \textit{decideOnForward}(i, j) \\
& \vee \textit{abortOnTimeout}(i)
\end{aligned}$$

$$\textit{parProgNNB} \triangleq \exists i, j \in \textit{participants} : \textit{parDie}(i) \vee \textit{parProgNB}(i, j)$$

$$\textit{progNNB} \triangleq \textit{parProgNNB} \vee \textit{coordProgN}$$

$$\begin{aligned}
\textit{fairnessNB} \triangleq & \wedge \forall i \in \textit{participants} : \text{WF}_{\langle \textit{coordinator}, \textit{participant} \rangle}(\exists j \in \textit{participants} : \textit{parProgNB}(i, j)) \\
& \wedge \text{WF}_{\langle \textit{coordinator}, \textit{participant} \rangle}(\textit{coordProgB})
\end{aligned}$$

$$\textit{SpecNB} \triangleq \textit{InitNB} \wedge \square[\textit{progNNB}]_{\langle \textit{coordinator}, \textit{participant} \rangle} \wedge \textit{fairnessNB}$$


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